

ERRATA

Advanced Mathematics 2 for A Level

First edition - 2017 initial print

The following erratum was made on 06/Jan/2022

page 295 CHAPTER 13, second to last line on page should read:

DECIMAL SEARCH

In a decimal search we improve the accuracy of our solution by a decimal **place** each iteration.

We achieve this by performing 9 calculations equally spaced on the interval.

The following erratum was made on 11/May/2020

page 494 ANSWERS REVIEW SET 8A, question 13 c should read:

- 13** a concave up for $x \geq \frac{4}{3}$, concave down for $x \leq \frac{4}{3}$
 b concave up for $x \leq -3$,
 concave down for $-3 \leq x < 0$ and $x > 0$
 c concave up for $-4 < x \leq -2$ and $x > 0$,
 concave down for $x < -4$ and $-2 \leq x < 0$

The following erratum was made on 04/May/2020

page 502 ANSWERS EXERCISE 12C, question 2 parts e and f should read:

- 2** a $y = Ae^x$ b $y = \pm\sqrt{2x+c}$
 c $y = Ae^t + 4$ d $P = \left(\frac{3}{2}t + c\right)^2$
 e $Q = Ae^{2t} - \frac{3}{2}$ f $Q = -\frac{3}{2} \pm \sqrt{t+c}$

The following errata were made on 17/Sep/2019

page 305 CHAPTER 13, table at start of solution to example 6 should read:

$$n = 4, a = 2, b = 3, f(x) = 2x^2 + 3$$

$$h = \frac{b-a}{4} = 0.25$$

$$x_i = 2 + 0.25i$$

i	x_i	$f(x_i)$	x_{mid}	$f(x_{\text{mid}})$
0	2	11		
1	2.25	13.125	2.125	12.031 25
2	2.5	15.5	2.375	14.281 25
3	2.75	18.125	2.625	16.781 25
4	3	21	2.875	19.531 25

page 462 CHAPTER 19, last line of solution to example 7 should read:

Step 6: Since we have accepted H_0 , we conclude that the variables are not **negatively** correlated.

The following errata was made on 25/Jul/2019

page 187 **CHAPTER 8**, blue box should read:

- $f(x)$ is **strictly increasing** on S **if** $f'(x) > 0$ for all $x \in S$
- $f(x)$ is **strictly decreasing** on S **if** $f'(x) < 0$ for all $x \in S$.

page 223 **CHAPTER 9**, text above blue box should read:

$$\text{For } x < 0, \frac{d}{dx}(\ln(-x) + c) = \frac{-1}{-x} = \frac{1}{x}$$
$$\therefore \int \frac{1}{x} dx = \begin{cases} \ln x + c & \text{if } x > 0 \\ \ln(-x) + c & \text{if } x < 0 \end{cases}$$
$$\therefore \int \frac{1}{x} dx = \ln |x| + c, \quad x \neq 0$$

page 227 **CHAPTER 9**, blue box should read:

$$\therefore \int (ax + b)^n dx = \frac{1}{a} \frac{(ax + b)^{n+1}}{(n+1)} + c \quad \text{for } n \neq -1, \quad a \neq 0.$$

page 248 **CHAPTER 10**, second to last line in example 10 should read:

Example 10

Self Tutor

Find $\int e^x \sin x dx$.

...

$$\therefore 2 \int e^x \sin x dx = -e^x \cos x + e^x \sin x + c$$

$$\therefore \int e^x \sin x dx = \frac{1}{2} e^x (\sin x - \cos x) + c$$

page 265 **EXERCISE 11D**, question 4 function should read:

- 4 The rate of power consumption of the United Kingdom can be modelled by the function

$$E(t) = 13 \sin\left(\frac{(t+3)\pi}{3}\right) + 70 \cos\left(\frac{(t-1)\pi}{6}\right) + 196 \quad \text{TWh per month}$$

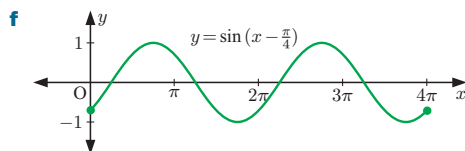
page 463 **EXERCISE 19D**, question 5 table should read:

The critical regions for a test of $H_0: \rho = 0$ against $H_1: \rho \neq 0$ for various significance levels are shown in the table alongside.

- Use technology to calculate the value of the test statistic for this hypothesis test.
- Use the critical regions to determine the significance level(s) for which H_0 will be rejected.
- Check your answer to **b** using the p -value.

α	Critical region
0.1	$(-\infty, -1.83] \cup [1.83, \infty)$
0.05	$(-\infty, -2.26] \cup [2.26, \infty)$
0.02	$(-\infty, -2.82] \cup [2.82, \infty)$
0.01	$(-\infty, -3.25] \cup [3.25, \infty)$

page 475 **ANSWERS EXERCISE 4A**, question **6 f** should have diagram:



page 480 **ANSWERS REVIEW SET 4A**, question **6 d** should read:

- d** A vertical dilation with scale factor 2, then a horizontal dilation with scale factor 2, then a translation $\frac{\pi}{4}$ units right and $\frac{1}{2}$ unit upwards.

page 483 **ANSWERS EXERCISE 6B**, question **7** should have correct labels on diagram:

- 7** No, we could find another solution by reversing the 2s and 3s. So, the solution is not unique, and the sudoku would not be well-posed.

		3	2						
		2	3						

page 501 **ANSWERS EXERCISE 11D**, question **3 b** should be in units instead of units²:

- 3 a** C_1 is $y = 3 \sin \frac{\pi t}{10}$, C_2 is $y = \sin \frac{\pi t}{10}$ **b** $\frac{40}{\pi}$ units

page 503 **ANSWERS EXERCISE 12D**, question **5 a** should read:

5 a $N \approx \frac{10^{30}}{1 + (5 \times 10^{27} - 1)e^{-kt}}$

page 504 **ANSWERS REVIEW SET 12B**, question **6 a** should read:

6 a $y = \left(\frac{1}{2}x \pm 2\right)^2$

The following erratum was made on 29/Nov/2018

page 172 **CHAPTER 7**, add line to explanation and add bubble text:

A more useful method for solving this type of problem is **implicit differentiation**.

If we are given an implicit relation between y and x and we want to find $\frac{dy}{dx}$, we can differentiate both sides of the equation with respect to x , applying the chain, product, quotient, and any other rules as appropriate. This will generate terms containing $\frac{dy}{dx}$, and we then proceed to make $\frac{dy}{dx}$ the subject of the equation.

Using the chain rule, $\frac{d}{dx}(y^n) = \frac{d}{dy}(y^n) \times \frac{dy}{dx}$

$\therefore \frac{d}{dx}(y^n) = ny^{n-1} \frac{dy}{dx}$

For example, if $x^2 + y^2 = 4$, then $\frac{d}{dx}(x^2 + y^2) = \frac{d}{dx}(4)$

$$\therefore 2x + 2y \frac{dy}{dx} = 0$$

$$\therefore \frac{dy}{dx} = -\frac{x}{y}$$

$\frac{d}{dx}(\dots)$ is read as
“dee by dee x of ...”



The following errata were made on 23/Nov/2018

page 39 CHAPTER 1, blue box should read:

For $n \in \mathbb{Z}^+$,

$$\begin{aligned}(a+b)^n &= a^n + \binom{n}{1}a^{n-1}b + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n \\ &= \sum_{r=0}^n \binom{n}{r}a^{n-r}b^r\end{aligned}$$

where $\binom{n}{r} = \frac{n!}{r!(n-r)!}$ is the **binomial coefficient** for $n \in \mathbb{Z}^+$, $r \in \mathbb{Z}_0^+$, $r \leq n$.

The **general term** or **$(r+1)$ th term** in the binomial expansion is $T_{r+1} = \binom{n}{r}a^{n-r}b^r$.

page 495 ANSWERS REVIEW SET 8B, question 10 a should have correct sign diagram:

10 a

$\begin{array}{c} - & - & - \\ | & | & | \\ -2 & & 4 \\ \hline & + & \\ x \end{array}$

The following errata were made on 05/Oct/2018

page 7 **GRAPHICS CALCULATOR INSTRUCTIONS**, Calculator instructions for Casio fx-991EX are also available.

page 41 **CHAPTER 1**, blue boxes should read:

For $n \in \mathbb{Q}$, $(a + b)^n = \sum_{r=0}^{\infty} \binom{n}{r} a^{n-r} b^r$

where $\binom{n}{r} = \frac{n(n-1)(n-2)\dots(n-r+1)}{r!}$ is the **binomial coefficient** for $n \in \mathbb{Q}$, $r \in \mathbb{Z}^+$, and $\binom{n}{0} = 1$.

....

For $n \in \mathbb{Q}$, $(a + bx)^n = a^n \sum_{r=0}^{\infty} \binom{n}{r} \left(\frac{bx}{a}\right)^r$

where $\binom{n}{r} = \frac{n(n-1)(n-2)\dots(n-r+1)}{r!}$ is the **binomial coefficient** for $n \in \mathbb{Q}$, $r \in \mathbb{Z}^+$, and $\binom{n}{0} = 1$.

The expansion **converges** for x such that $\left|\frac{bx}{a}\right| < 1$.

$\left|\frac{bx}{a}\right| < 1$
means
 $-\left|\frac{a}{b}\right| < x < \left|\frac{a}{b}\right|$.



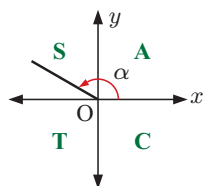
page 120 **CHAPTER 5 EXAMPLE 8**, should read:

Example 8

Self Tutor

If $\sin \alpha = \frac{5}{13}$ where $\frac{\pi}{2} < \alpha < \pi$, find the exact value of: **a** $\sin 2\alpha$ **b** $\tan 2\alpha$.

α is in quadrant 2, so $\cos \alpha$ is negative.



a $\sin 2\alpha = 2 \sin \alpha \cos \alpha$
 $\therefore \sin 2\alpha = 2\left(\frac{5}{13}\right)\left(-\frac{12}{13}\right)$
 $= -\frac{120}{169}$

Now $\cos^2 \alpha + \sin^2 \alpha = 1$

$\therefore \cos^2 \alpha + \frac{25}{169} = 1$
 $\therefore \cos^2 \alpha = \frac{144}{169}$
 $\therefore \cos \alpha = \pm \frac{12}{13}$
 $\therefore \cos \alpha = -\frac{12}{13}$ {as $\frac{\pi}{2} < \alpha < \pi$ }

b $\tan \alpha = \frac{\sin \alpha}{\cos \alpha} = -\frac{5}{12}$
 $\therefore \tan 2\alpha = \frac{2 \tan \alpha}{1 - \tan^2 \alpha}$
 $= \frac{2\left(-\frac{5}{12}\right)}{1 - \left(-\frac{5}{12}\right)^2}$
 $= \frac{-\frac{5}{6}}{1 - \frac{25}{144}}$
 $= -\frac{120}{119}$

page 308 **CHAPTER 13 EXAMPLE 7**, table in solution should read:

$n = 6$, $a = 1$, $b = 2$, $f(x) = \sqrt{6 - x^2}$

$h = \frac{b-a}{n} = \frac{1}{6}$

$x_i = 1 + \frac{1}{6}i$

i	x_i	$f(x_i)$
0	1	2.236 068
1	$1\frac{1}{6}$	2.153 808
2	$1\frac{1}{3}$	2.054 805
3	$1\frac{1}{2}$	1.936 492
4	$1\frac{2}{3}$	1.795 055
5	$1\frac{5}{6}$	1.624 466
6	2	1.414 214

GRAPHING PACKAGE

