

6 Consider an anticlockwise rotation about the origin through angle θ . Suppose an object point is located by a position vector which is an eigenvector \mathbf{v} of the transformation matrix $\mathbf{A} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$.

HISTORICAL NOTE

EULER'S BEAUTIFUL EQUATION

One of the most remarkable results in mathematics is known as **Euler's beautiful equation** $e^{i\pi} = -1$ named after **Leonhard Euler**.

It is called beautiful because it links together three great constants of mathematics: Euler's **number** e , the imaginary number i , and the ratio of a circle's circumference to its diameter, which is π .

Harvard lecturer **Benjamin Pierce** said of $e^{i\pi} = -1$,

"Gentlemen, that is surely true, it is absolutely paradoxical; we cannot understand it, and we don't know what it means, but we have proved it, and therefore we know it must be the truth."

Example 5

Self Tutor

Find the nature of the transformation with equations:

$$\begin{cases} x' = \frac{-3x - 4y}{5} \\ y' = \frac{-4x + 3y}{5} \end{cases}$$

$$\mathbf{A} = \begin{pmatrix} -\frac{3}{5} & -\frac{4}{5} \\ -\frac{4}{5} & \frac{3}{5} \end{pmatrix} \text{ where } |\mathbf{A}| = -\left(\frac{3}{5}\right)^2 - \left(-\frac{4}{5}\right)^2 = -1.$$

Since \mathbf{A} has the form $\begin{pmatrix} a & b \\ b & -a \end{pmatrix}$ and $|\mathbf{A}| = -1$,

\mathbf{A} is a reflection matrix where $\cos 2\alpha = -\frac{3}{5}$ and $\sin 2\alpha = -\frac{4}{5}$.

$$\therefore \tan 2\alpha = \frac{4}{3}, \quad \pi < 2\alpha < \frac{3\pi}{2}$$

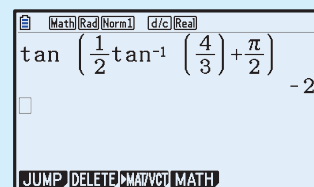
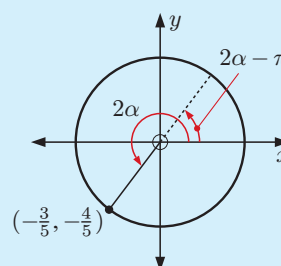
$$\therefore \tan(2\alpha - \pi) = \frac{4}{3}, \quad 0 < 2\alpha - \pi < \frac{\pi}{2}$$

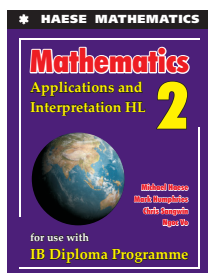
$$\therefore 2\alpha - \pi = \tan^{-1}\left(\frac{4}{3}\right)$$

$$\therefore \alpha = \frac{1}{2} \tan^{-1}\left(\frac{4}{3}\right) + \frac{\pi}{2}$$

$$\therefore \tan \alpha = -2$$

\therefore the transformation is a reflection in the line $y = -2x$.





ERRATA

Mathematics: Applications and Interpretation HL

First edition - 2020 first reprint

The following erratum was made on 18/Aug/2021

page 650 **CHAPTER 25** Example 5, last line of question should read:

Example 5

Self Tutor

The marginal cost of producing x urns per week is given by

$$\frac{dC}{dx} = 2.15 - 0.02x + 0.00036x^2 \text{ pounds per urn provided } 0 \leq x \leq 120.$$

The initial costs before production starts are £185.

Find the total cost of producing 100 urns per week.

....

The following erratum was made on 13/Apr/2021

page 898 **ANSWERS EXERCISE 12F.3** Question 4 c, should read:

4 a $A^2 = \begin{pmatrix} \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} \end{pmatrix}$ b false as $A(A - I) = O$ does not imply that $A = O$ or $A - I = O$

c $\begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}, \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, \begin{pmatrix} 0 & 0 \\ c & 1 \end{pmatrix}, \begin{pmatrix} 1 & 0 \\ c & 0 \end{pmatrix} (c \in \mathbb{R}),$
 $\begin{pmatrix} a & b \\ \frac{a-a^2}{b} & 1-a \end{pmatrix} (b \neq 0)$

The following errata were made on 04/Mar/2021

page 385 **CHAPTER 15** Section D, first blue box should read:

An **adjacency matrix** is a matrix which shows how the **vertices** of a network are connected.

page 434 **CHAPTER 16** Example 5, question should read:

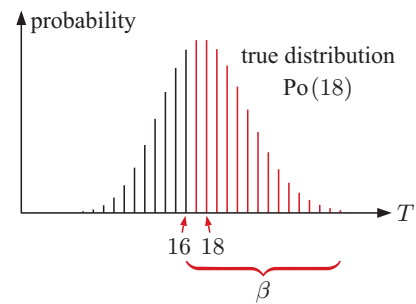
Redraw this Voronoi diagram with an additional site at $E(-2, 1)$.

The following errata were made on 27/Jan/2021

page 822 **CHAPTER 30** Example 14, diagram of solution to part c should have 16 column coloured black:

- c A Type II error is accepting H_0 when H_0 is in fact false. This means accepting $\lambda = 2$ when in fact $\lambda = 1.5$.

$$\begin{aligned} & P(\text{Type II error}) \\ &= P(\text{Retain } H_0 \mid H_0 \text{ false}) \\ &= P(T > 16 \mid T \sim \text{Po}(18)) \\ &\approx 0.625 \end{aligned}$$



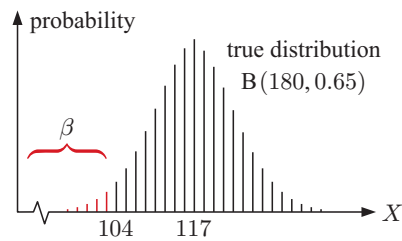
page 823 **CHAPTER 30** Example 15, diagram of solution to part c should have 104 label in correct position:

- c A Type II error means deciding the coin is fair when it is in fact biased.

If $p = 0.65$, then $X \sim B(180, 0.65)$.

$$\begin{aligned} \therefore \beta &= P(\text{Type II error}) \\ &= P(\text{Retain } H_0 \mid H_0 \text{ false}) \\ &= P(X < 104 \mid X \sim B(180, 0.65)) \\ &\approx 0.0184 \end{aligned}$$

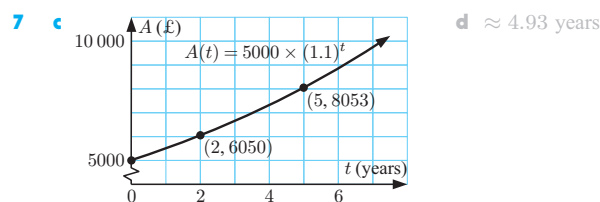
$$\therefore \text{the power of the test} = 1 - \beta \approx 0.9816$$



b Hence estimate g , the acceleration due to gravity for an object at low altitude.

- 6** A survey was conducted to determine whether the use of social media is linked to the amount of exercise a person gets. The table below summarises the results from a survey.
Test at a 5% level of significance whether the variables are related.

		Social media (y hours per week)			
		$y < 2$	$2 \leq y < 6$	$6 \leq y < 10$	$y \geq 10$
Exercise (x hours per week)	$x < 2$	5	13	11	21
	$2 \leq x < 4$	16	22	18	14
	$4 \leq x < 6$	20	26	16	9
	$x \geq 6$	15	8	11	3



- 3** **a** truck A: $\begin{pmatrix} -72 \\ 54 \end{pmatrix}$, truck B: $\begin{pmatrix} -75 \\ 40 \end{pmatrix}$
b truck A: 1:30 pm, truck B: 2:00 pm
c **i** $\approx 12:41$ pm **ii** ≈ 40.9 km

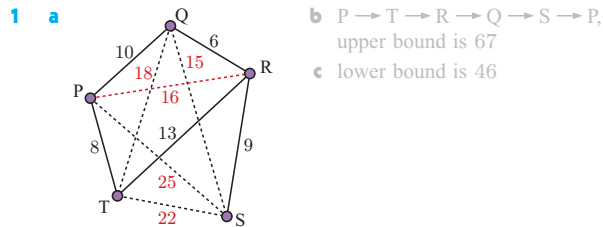
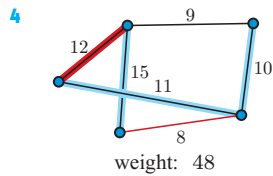
- 6** **a** Jove **b** $\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} -4 \\ -1 \end{pmatrix} + t \begin{pmatrix} \frac{3}{2} \\ -2 \end{pmatrix}$ **c** $(-1, -5)$
d No; Jove passes through the intersection point after **2 seconds**, and Fiona passes through it after 6 seconds.

11 $A = \frac{\sin \frac{\pi}{5} + \cos \frac{\pi}{5}}{\sin \frac{\pi}{7} + \cos \frac{\pi}{7}}$, $B = \frac{\sin \frac{\pi}{7} \cos \frac{\pi}{5} - \cos \frac{\pi}{7} \sin \frac{\pi}{5}}{\sin \frac{\pi}{7} + \cos \frac{\pi}{7}}$

- 5** **a** Eigenvalues are 3 and -2 .
 For $\lambda = 3$, $\mathbf{x} = \begin{pmatrix} 1 \\ -4 \end{pmatrix} t$, $t \neq 0$.
 For $\lambda = -2$, $\mathbf{x} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} t$, $t \neq 0$.

1 **a** $\lambda^2 + \lambda - 4$ **b** $-\frac{1}{2} \pm \frac{\sqrt{17}}{2}$

- 6** **a** $\lambda_1 = 5$, $\mathbf{x}_1 = \begin{pmatrix} -1 \\ 5 \end{pmatrix}$, $\lambda_2 = 4$, $\mathbf{x}_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$
b $\mathbf{P} = \begin{pmatrix} -1 & 0 \\ 5 & 1 \end{pmatrix}$, $\mathbf{P}^{-1}\mathbf{B}\mathbf{P} = \begin{pmatrix} 5 & 0 \\ 0 & 4 \end{pmatrix}$
c **i** $\mathbf{B}^3 = \begin{pmatrix} 5^3 & 0 \\ -5^4 + 5 \times 4^3 & 4^3 \end{pmatrix} = \begin{pmatrix} 125 & 0 \\ -305 & 64 \end{pmatrix}$
ii $\mathbf{B}^6 = \begin{pmatrix} 5^6 & 0 \\ -5^7 + 5 \times 4^6 & 4^6 \end{pmatrix} = \begin{pmatrix} 15\,625 & 0 \\ -57\,645 & 4096 \end{pmatrix}$



- 2 a** $C(x) \approx -0.178x^3 + 15.3x^2 + 3280x + 24\,500$
b €331 000
3 a $P(0) = 21.5 \quad \therefore d = 21.5$
b $P'(t) = 3at^2 + 2bt + c$ **c** $t = 15$
d $3375a + 225b + 15c = 5$
 $125\,000a + 2500b + 50c = -13.9$
 $675a + 30b + c = 0$
 $\therefore P(t) \approx 0.000\,136t^3 - 0.0263t^2 + 0.697t + 21.5$
e i ≈ 22.4 million **ii** ≈ -1.98 million
f The model provided a reasonable estimate when interpolating between data points. The extrapolation in **e ii** however predicted a negative population, which is not possible.

- 5 b** $\dot{x}(t) = 1 - \frac{2}{2t+1} \text{ cm s}^{-1}$
c i $t > \frac{1}{2}$ **ii** $0 \leq t < \frac{1}{2}$ **d** $\ddot{x}(t) = \frac{4}{(2t+1)^2}$
f $\frac{4}{25} \text{ cm s}^{-2}$ **g** $1 + \ln\left(\frac{4}{5}\right) \approx 0.777 \text{ cm}$

- 5 b ii** The particle initially moves to the left, and while $3 < s < 5$, $v < 0$ and $a > 0$. As time progresses, the particle approaches $s = 3$, and v and a approach 0.

- 2 a** $(11, -10)$ **b** $\left(\frac{3}{\sqrt{t+1}}, \frac{4}{t}\right)$ **c** 5 m s^{-1}
d The truck decreases to a speed of 4 m s^{-1} . **e** $t = \frac{19}{17} \text{ s}$

page 948 **ANSWERS EXERCISE 25D** Question **4 d**, should read:

4 a $y = \sqrt[3]{\frac{9}{2}x^2 + 1}$ **b** $y = \frac{1}{36}(x - 26)^2$
c $y = e^{x + \frac{1}{3}x^3}$ **d** $y = \sin^{-1}\left(\frac{3}{2}x^2 - \frac{3}{2}\right)$
e $y = \left(\frac{9}{2}\sin 2x + 3\sqrt{3}\right)^{\frac{2}{3}}$

page 949 **ANSWERS REVIEW SET 25B** Question **6 a**, should read:

6 a $y = \left(\frac{1}{2}x + 2\right)^2$ **b** $y = e^{\sin x - 3}$

page 953 **ANSWERS REVIEW SET 26B** Question **4 d**, should read:

4 d (0.06, 6)

page 954 **ANSWERS EXERCISE 27D** Question **8 a i**, should read:

8 a i Y would have the greater mean as, on average, we are more likely to obtain higher values from the maximum of two rolls than from a single roll.

page 956 **ANSWERS REVIEW SET 27A** Question **14 a**, should read:

14 a ≈ 0.824 **b** ≈ 0.0293 **c** ≈ 0.450

page 959 **ANSWERS EXERCISE 29A** Question **4 b**, should read:

- 4 a** As $\sum P(x) = 1$ in each distribution, each is a well defined probability distribution.
b i $E(X) = 2.5$, $\sigma(X) = \sqrt{5.25} \approx 2.29$
ii $E(Y) = 2.2$, $\sigma(Y) = \sqrt{9.16} \approx 3.03$
c $-\$0.30$ or -30 cents
d No; the expected gain from playing this game is negative.

page 960 **ANSWERS EXERCISE 29C** Question **5 a**, should read:

5 a ≈ 0.00400 **b** ≈ 0.00110

page 960 **ANSWERS REVIEW SET 29A** Question **9 a**, should read:

9 a $s^2 \approx 16.4$ **b i** $124.75 \leq \mu \leq 129.24$ **ii** $k \approx 93.0$

page 961 **ANSWERS REVIEW SET 29B** Question **9 c**, should read:

9 a ≈ 0.0515 **b** ≈ 0.0299 **c** 601.3 mL

page 963 **ANSWERS REVIEW SET 30A** Question **13 c**, should read:

13 a i $\{x \mid x \geq 13\}$ **ii** $\{x \mid x \leq 12\}$
b ≈ 0.0253 or $\approx 2.53\%$ **c** ≈ 0.0898

page 964 **ANSWERS EXERCISE 31B** Question **2 b**, should read:

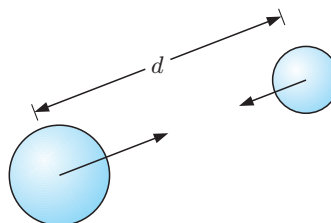
- 2 a** ≈ 0.885 accidents per week
b $\chi^2_{\text{calc}} \approx 11.5$, $\text{df} = 2$, $p\text{-value} \approx 0.00325$
Since $p\text{-value} < 0.05$, we conclude that the data does not come from a Poisson distribution at a 5% significance level.

- 4 e $\chi^2_{\text{calc}} \approx 9.37$, $df = 4$, $p\text{-value} \approx 0.0248$
 Since $p\text{-value} > 0.01$, there is insufficient evidence to reject H_0 at a 1% level of significance. We conclude that the data is normally distributed.

The following errata were made on 06/Oct/2020

page 192 **REVIEW SET 8B** Question 6, table should read:

- 6 Gravity is the force of attraction which exists between any two objects in the universe. The force of attraction F between two spherical masses at various distances d apart is shown below:

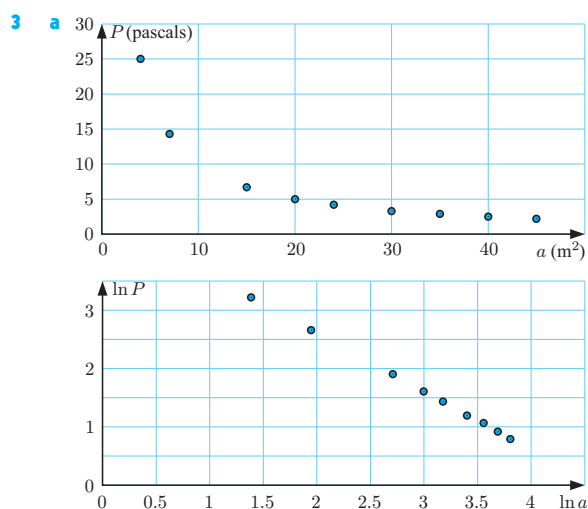


d (cm)	24	26	28	30	32	34	36	38	40
F (newtons)	0.237	0.202	0.174	0.152	0.133	0.118	0.105	0.095	0.085

page 878 **ANSWERS REVIEW SET 7B** Question 8 e, should read:

- 8 e $r^2 \approx 0.346$; approximately 34.6% of the variation in *sales* can be explained by the variation in *price*.
 So, the linear model does not fit the data very well.

page 879 **ANSWERS EXERCISE 8C** Question 3, both graphs should belong to part a:



- b The scatter diagram of $\ln P$ against $\ln a$ appears to be linear, so a power model is appropriate.

page 883 **ANSWERS REVIEW SET 8B** Questions 4 b and 6, should read:

- 4 a The scatter diagram of b against $\ln P$ appears to be linear.
 b $b \approx 9.03 - 0.441 \ln P$ $c \approx 31.8$ torr
- 6 a $F \approx 138 \times d^{-2.00}$, the graph of $\ln F$ against $\ln d$ appears to be linear.
 b i ≈ 0.162 newtons ii ≈ 0.342 newtons
 iii $\approx 5.39 \times 10^{-6}$ newtons

page 894 **ANSWERS EXERCISE 11H.1** Question 5 b i, should read:

- 5 a $z_1 = 4 \operatorname{cis} \frac{2\pi}{3}$
 b i $z_2 = 8 \operatorname{cis} \left(-\frac{5\pi}{6}\right)$ ii $z_2 = -4\sqrt{3} - 4i$

The following errata were made on 21/Sep/2020

page 864 **ANSWERS EXERCISE 2E** Question **3 d**, should read:

- 3 d** Our scale in **c** is obtained by translating the scale in **a** ≈ 6.77 units left. This occurs since $\log\left(\frac{P}{P_S}\right) = \log P - \log P_S$.

page 865 **ANSWERS EXERCISE 3B** Question **13 b**, should read:

- 13 a** ≈ 4.40 hours (≈ 4 h 24 min 5 s) **b** $\approx 0.289\%$

page 866 **ANSWERS REVIEW SET 3B** Questions **1 b** and **3**, should read:

- 1 a** $14.85 \text{ s} < t < 14.95 \text{ s}$ **b** $6.69 \text{ m s}^{-1} < s < 6.73 \text{ m s}^{-1}$
2 $267.5 \text{ cm}^2 < A < 355.5 \text{ cm}^2$ **3** $59.6 \text{ km} < D < 60.2 \text{ km}$

page 897 **ANSWERS EXERCISE 12A** Question **5**, should read:

- 5** pies pasties rolls buns
 $\begin{pmatrix} 40 & 50 & 55 & 40 \\ 25 & 65 & 44 & 30 \\ 35 & 40 & 40 & 35 \\ 35 & 40 & 35 & 50 \end{pmatrix} \begin{matrix} \text{Friday} \\ \text{Saturday} \\ \text{Sunday} \\ \text{Monday} \end{matrix} \quad (\text{in dozens})$

The following errata were made on 08/Sep/2020

page 60 CHAPTER 2 INVESTIGATION 2 Question 1, should read:

What to do:

- 1 Print the graph. Mark, as accurately as possible, the values on the x -axis corresponding to y being 1, 2, 3, 4, ..., 9, and 10, 20, 30, 40, ..., 90.

page 75 REVIEW SET 3A Question 3, should read:

- 3 A triangular garden is measured to have sides of length 9 m, 12 m, and 14 m, rounded to the nearest metre. Find the range of possible values for the area A of the garden.

page 187 CHAPTER 8 ACTIVITY 3 Question 1 c, should read:

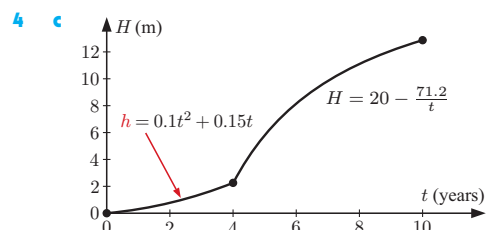
What to do:

- 1 c How can the *precision* of the estimate be improved in the spreadsheet?

page 865 ANSWERS REVIEW SET 3A Question 3, should read:

- 2 $48 \text{ cm} < P < 52 \text{ cm}$ 3 $48.6 \text{ m}^2 < A < 58.7 \text{ m}^2$

page 932 ANSWERS EXERCISE 20A Question 4 c, diagram should have correct label:



The following errata were made on 18/Aug/2020

page 132 REVIEW SET 6A Question 10, first sentence should read:

- 10 Kelly makes glass regular pyramids of height h cm with equal edge lengths. She suspects that the volume of glass $V \text{ cm}^3$ she uses is directly proportional to a power of h , so $V \propto h^n$. A table of volumes for various heights is shown below.

page 919 ANSWERS REVIEW SET 16B Question 4 a, should read:

- 4 a There is a cell with no corresponding site. b (3, 1)

The following erratum was made on 27/Jul/2020

page 872 ANSWERS REVIEW SET 6A Question 10 a, replace with:

- 10 a If the height of a regular pyramid increases, then each side length also increases.
This means the pyramid gets larger in all 3 dimensions as the height increases, so we should expect that V is directly proportional to h^3 .
- b $V = \frac{2}{5}h^3$ c $\frac{2}{5} \times 4^3 = 25.6$ ✓ $\frac{2}{5} \times 6^3 = 86.4$ ✓
- d i $V = 204.8$ ii $h = 5$

The following erratum was made on 16/Jul/2020

page 932 **ANSWERS EXERCISE 20A** Question **4 b iii**, should read:

- 4 a i** $\frac{dh}{dt} = 0.2t + 0.15$ metres per year
ii 0.35 m per year **iii** after 3 years **iv** 2.2 m
- b i** $k = 71.2$ **ii** $\frac{dH}{dt} = \frac{71.2}{t^2}$
- iii** Yes, since $\frac{dh}{dt} \neq \frac{dH}{dt}$ when $t = 4$.

The following erratum was made on 17/Jun/2020

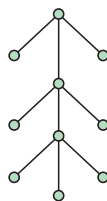
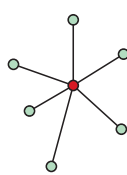
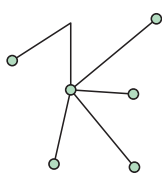
page 35 **CHAPTER 1 INVESTIGATION 2** Question **5**, should read:

- 5** For continuous growth, $u_n = u_0 e^{rt}$ where u_0 is the initial amount, r is the annual percentage rate, and t is the number of years.
- Use this formula to find the final amount if \$1000 is invested for **1 year** at a fixed rate of 6% per annum, where the interest is paid continuously.

The following erratum was made on 27/May/2020

page 394 **SECTION 18F** Second example of trees should include vertex shown:

Some examples of trees are shown below:



Every connected simple graph has a subgraph which is a tree.



The following erratum was made on 13/May/2020

page 931 **ANSWERS REVIEW SET 19B** Question **18 b**, should read:

- 18 a** $0 \leq x \leq \frac{\pi}{2}$ and $\frac{3\pi}{2} \leq x \leq 2\pi$
- b** $f'(x) = -\frac{\sin x}{2\sqrt{\cos x}}$, increasing for $\frac{3\pi}{2} \leq x \leq 2\pi$,
decreasing for $0 \leq x \leq \frac{\pi}{2}$

The following erratum was made on 27/Apr/2020

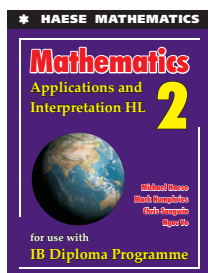
page 948 **ANSWERS EXERCISE 25D** Question **2 f**, should read:

- 2 a** $y = Ae^x$ **b** $y = \pm\sqrt{2x+c}$
c $y = Ae^t + 4$ **d** $P = \left(\frac{3}{2}t + c\right)^2$
e $Q = Ae^{2t} - \frac{3}{2}$ **f** $Q = -\frac{3}{2} \pm \sqrt{t+c}$

The following erratum was made on 24/Apr/2020

page 959 **ANSWERS EXERCISE 29A** Question **2**, should read:

- 2 a** $E(X + 2Y) = 15.2$, $\sigma(X + 2Y) \approx 2.07$
b $E(Y - X) = 1.9$, $\sigma(Y - X) \approx 1.07$
c $E(3X - 2Y) = 0$, $\sigma(3X - 2Y) \approx 2.26$



ERRATA

Mathematics: Applications and Interpretation HL

First edition - 2019 initial print

The following errata were made on 24/Apr/2020

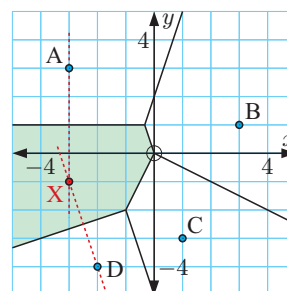
page 432 **SECTION 16B** Example 4, last line of solution should read:

The missing site X must lie in the shaded cell, as this cell currently has no site.

Now $PB(A, X)$ is horizontal, and $PB(D, X)$ has gradient $\frac{1}{3}$.

$\therefore [AX]$ is vertical and $[DX]$ has gradient -3 .

If we draw lines (AX) and (DX) through A and D respectively, their intersection must be point X. We observe that X has coordinates $(-3, -1)$.



page 519 **REVIEW SET 19A** Question 4 is a duplicate of RS 18A Q7 p492, replace with:

4 Find all points on the curve $y = 4x^3 + 6x^2 - 13x + 1$ where the gradient of the tangent is 11.

page 718 **CHAPTER 27 INVESTIGATION 2** Question 1, change for simplicity:

What to do:

1 Click on the icon to access the demonstration. It shows the graph of the binomial distribution for $X \sim B(n, p)$. Set $n = 25$ and $p = 0.1$.

- What is the mode of X ?
- Describe the shape of the distribution.



page 724 **SECTION 27I**, first line on page should read:

In factorial notation we use $x!$ to denote the **product** of the first x integers $x \times (x-1) \times \dots \times 3 \times 2 \times 1$. We also define $0! = 1$.

page 789 **SECTION 30B**, bottom blue box *Step 5* should read:

Step 5: Reject H_0 if $p\text{-value} \leq \alpha$, otherwise accept H_0 .

page 798 **SECTION 30D**, blue box *Step 5* should read:

Step 5: Reject H_0 if $p\text{-value} \leq \alpha$ or if $t \in \mathcal{C}$, otherwise accept H_0 .

POISSON RANDOM SAMPLES

Suppose the population has a Poisson distribution with an unknown mean λ . We want to test the null hypothesis $H_0: \lambda = \lambda_0$.

Consider a random sample of n independent and identically distributed observations from this population, $\{X_1, \dots, X_n\}$.

We have already seen that an estimator for the population mean is the sample mean $\bar{X}_n = \frac{1}{n} \sum_{i=1}^n X_i$.

We will therefore consider $n\bar{X}_n = \sum_{i=1}^n X_i$ when we choose our test statistic.

Step 5: Reject H_0 if $p\text{-value} \leq \alpha$, otherwise accept H_0 .

Step 5: Reject H_0 if $p\text{-value} \leq \alpha$, otherwise accept H_0 .

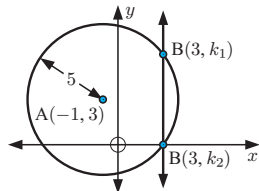
Step 6: Reject H_0 if $p\text{-value} \leq \alpha$ or if $\chi_{\text{calc}}^2 \geq \chi_{\text{crit}}^2$, otherwise accept H_0 .

Step 5: Since $p\text{-value} > 0.05 = \alpha$, we do not have enough evidence to reject H_0 in favour of H_1 on a 5% significance level. We therefore accept H_0 .

Step 6: Since we have accepted H_0 , we conclude that the variables are not **negatively** correlated.

14 a $\vec{AB} = \begin{pmatrix} 4 \\ k-3 \end{pmatrix}$, $|\vec{AB}| = \sqrt{16 + (k-3)^2}$ units

b $k = 0$ or 6 c



3 c At $t = 5$ s, the stone is 367.5 m above the ground and moving upward at 49 m s^{-1} . It has acceleration -9.8 m s^{-2} .
At $t = 12$ s, the stone is 470.4 m above the ground and moving downward at 19.6 m s^{-1} . It has acceleration -9.8 m s^{-2} .

1 c i $\mu = 4.8$, $\sigma \approx 0.980$

10 a $\mu \approx 176 \text{ g}$, $\sigma \approx 24 \text{ g}$ b $\approx 81.85\%$

9 a $\approx 10.3\%$ b ≈ 0.456 10 a $\approx 84.1\%$ b ≈ 0.879

The following erratum was made on 13/Nov/2019

page 921 **ANSWERS EXERCISE 17C.2** Question **2 b**, last line of part **ii** should instead belong to part **i**:

- 2 b i** $\lim_{x \rightarrow -\infty} (e^x - 6) = -6$
 $y = -6$ is a horizontal asymptote of $y = e^x - 6$.
ii $\lim_{x \rightarrow \infty} (e^x - 6)$ does not exist

The following erratum was made on 22/Oct/2019

page 371 **SECTION 14G ACTIVITY 3 FRACTAL GEOMETRY** Part 2, should read:

PART 2: VON KOCH'S CURVE

The von Koch curve begins with the line segment [OD] shown. Its first iteration, shown in blue, is generated by the affine IFS $\{f_1, f_2, f_3, f_4\}$ where:

- f_1 is the transformation mapping [OD] to [OA]
- f_2 is the transformation mapping [OD] to [AB]
- f_3 is the transformation mapping [OD] to [BC]
- f_4 is the transformation mapping [OD] to [CD].

What to do:

- 1** Describe in words, the transformation:

- | | | |
|-----------------------|-----------------------|------------------------|
| a [OD] to [OA] | b [OA] to [OE] | c [OE] to [AB] |
| d [OA] to [OF] | e [OF] to [BC] | f [OA] to [CD]. |

