

ERRATA

Mathematics: Applications and Interpretation SL

First edition - 2020 first reprint

The following erratum was made on 03/Mar/2021

page 428 **CHAPTER 17 EXAMPLE 5** Question, should read::

Redraw this Voronoi diagram with an additional site at $E(-2, 1)$.

The following erratum was made on 21/Sep/2020

page 443 **ANSWERS REVIEW SET 1B** Question **6 b**, should read:

6 a $14.85 \text{ s} < t < 14.95 \text{ s}$ **b** $6.69 \text{ m s}^{-1} < s < 6.73 \text{ m s}^{-1}$

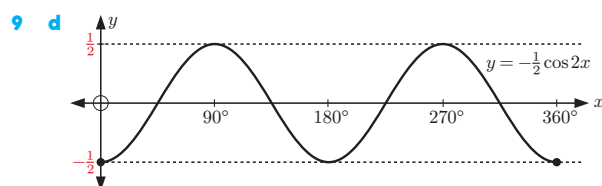
The following erratum was made on 16/Sep/2020

page 426 **CHAPTER 17 EXAMPLE 4** Solution, last line should read:

If we draw lines (AX) and (DX) through A and D respectively, their intersection must be point X. We observe that X has coordinates $(-3, -1)$.

The following erratum was made on 08/Sep/2020

page 478 **ANSWERS REVIEW SET 9B** Question **9 d**, should read:



The following errata were made on 11/Aug/2020

page 181 **REVIEW SET 7B** Question **9**, first sentence should read:

- 9** Kelly makes glass regular pyramids of height h cm with equal edge lengths. She suspects that the volume of glass $V \text{ cm}^3$ she uses is directly proportional to a power of h , so $V \propto h^n$. A table of volumes for various heights is shown below.

page 290 **EXERCISE 12A.1** Question **7**, should read:

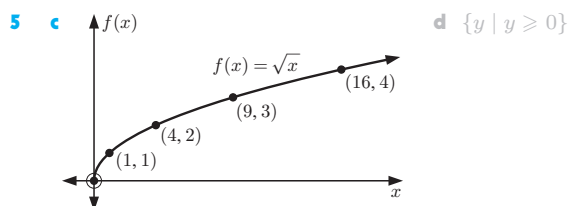
- 7** Joseph starts to pump air in his bicycle tyre. From the time 1 second after he starts pumping, the volume of air in the tyre is given by $V = -\frac{1200}{t} + 1380 \text{ cm}^3$, $t \geq 1$.
- a** Find $\frac{dV}{dt}$ and state its units.
 - b** At what rate is air being pumped into the tyre after:
 - i** 2 seconds
 - ii** 6 seconds?
 - c** Graph $V(t)$.
 - d** Discuss what happens to $\frac{dV}{dt}$ as time increases.

What to do:

Consider a multiple choice quiz with 10 questions. Each question has 4 choices, only 1 of which is correct.

The quiz is given to 150 people, and the number of correct answers for the participants is summarised in the table alongside.

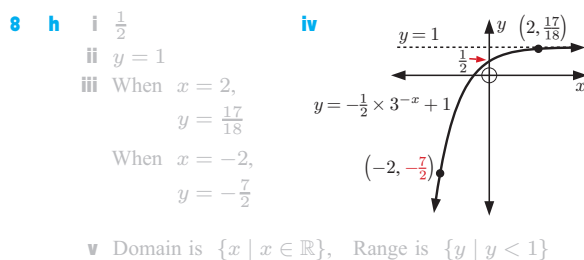
Number of correct answers	Frequency
0	6
1	13
2	33
3	45
4	30
5 or more	23



- 1 a -12
b i $\approx -1.05, 1.84, \text{ and } 6.20$
ii min. turning point $(0.225, -12.3)$,
max. turning point $(4.44, 25.1)$
2 a x-intercepts are ≈ -1.12 and ≈ 3.60 , y-intercept is -5
b max. turning point $(0.688, -3.54)$,
min. turning point $(-0.402, -5.76)$ and $(2.71, -15.2)$
c as $x \rightarrow \infty, y \rightarrow \infty$; as $x \rightarrow -\infty, y \rightarrow \infty$

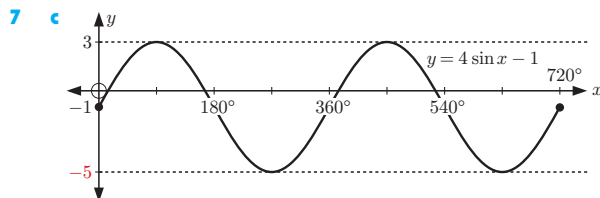
- 4 m iv Domain is $\{x \mid -5 \leq x \leq 5, x \neq -2\}$,
Range is $\{y \mid y \leq \frac{1}{3}\}$

- 9 a If the height of a regular pyramid increases, then each side length also increases. This means the pyramid gets larger in all 3 dimensions as the height increases, so we should expect that V is directly proportional to h^3 .



- 5 a $-1 \leq \sin \theta \leq 1$

page 478 **ANSWERS REVIEW SET 9B** Question **7 c**, diagram should read:



page 480 **ANSWERS EXERCISE 10G** Question **11**, should read:

11 $\frac{dC}{dx} = 7$ when $x = 1000$.

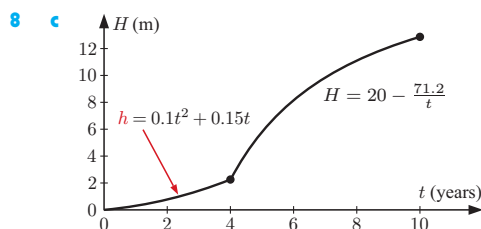
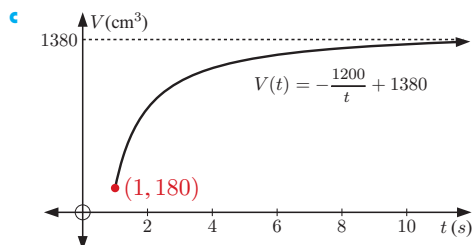
When 1000 toasters are being produced each week, the cost of production is increasing by £7 per toaster.

page 483 **ANSWERS REVIEW SET 11A** Question **12 a**, should include sign diagram:

12 a $f'(x) = 3 - \frac{48}{x^2}$

page 484 **ANSWERS EXERCISE 12A.1** Questions **7 a, c**, and **8 c**, diagrams should read:

7 a $\frac{1200}{t^2} \text{ cm}^3 \text{ s}^{-1}$ **b i** $300 \text{ cm}^3 \text{ s}^{-1}$ **ii** $33\frac{1}{3} \text{ cm}^3 \text{ s}^{-1}$



page 484 **ANSWERS EXERCISE 12A.2** Question **3 b**, should read:

- 3 a** $C(0) = \$14\,230$, which is the fixed operation cost without producing any items.
- b** $C'(x) = -0.000\,021\,6x^2 + 0.0122x + 18$
This is the rate at which the production cost (in dollars) is **changing** per item when x items are made. It gives an estimate of the cost of making the $(x + 1)$ th item each day.

page 485 **ANSWERS EXERCISE 12C** Question **2 b**, should read:

2 a $C(x) \approx -0.178x^3 + 15.3x^2 + 3280x + 24\,500$
b $\approx \text{€}331\,000$

page 492 **ANSWERS EXERCISE 15A.1** Question **2 c**, should read:

- 2 c** The times may be affected by:
- weather conditions
 - walking speed
 - physical fitness
 - traffic.

page 502 **ANSWERS REVIEW SET 17B** Question **4 a**, should read:

- 4 a** There is a **cell** with no corresponding site. **b** $(3, 1)$

The following errata were made on 16/Jun/2020

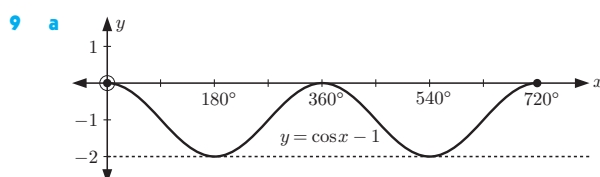
page 200 CHAPTER 8 INVESTIGATION 2 Question 3, should read:

- 3 Suppose u_0 is invested for t years at a **fixed percentage rate of r per year**, compounded N times per year.

page 201 CHAPTER 8 INVESTIGATION 2 Question 6, should read:

- 6 For continuous growth, $u_n = u_0 e^{rt}$ where u_0 is the initial amount, r is the annual percentage rate, and t is the number of years.
Use this formula to find the final amount if \$1000 is invested for **1 year** at a fixed rate of 6% per annum, where the interest is paid continuously. Compare this value with your calculations in 1.

page 475 ANSWERS EXERCISE 9D Question 9 a, diagram should be:



page 476 ANSWERS EXERCISE 9D Question 12 b, should read:

- 12 a 4 b **120°** c $\{y \mid -2 \leq y \leq 6\}$

The following errata were made on 29/Apr/2020

page 387 SECTION 16B, fifth step of summary should read:

SUMMARY OF STEPS FOR STUDENT'S t -TEST FOR A POPULATION MEAN

Step 1: State the **null hypothesis** $H_0: \mu = \mu_0$ and **alternative hypothesis** H_1 .

Step 2: State the **significance level** α .

Step 3: Calculate the value of the **test statistic** $t = \frac{\bar{x} - \mu_0}{\frac{s}{\sqrt{n}}}$.

Step 4: Calculate the **p-value** using $T \sim t_{n-1}$ as follows:

- If $H_1: \mu > \mu_0$, $p\text{-value} = P(T \geq t)$.
- If $H_1: \mu < \mu_0$, $p\text{-value} = P(T \leq t)$.
- If $H_1: \mu \neq \mu_0$, $p\text{-value} = 2 \times P(T \geq |t|)$.

Step 5: Reject H_0 if $p\text{-value} \leq \alpha$.

Step 6: Interpret your decision in the context of the problem. Write your conclusion in a sentence.

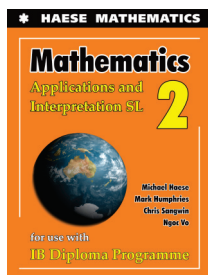
SUMMARY OF THE χ^2 GOODNESS OF FIT TEST

- Step 1:* State the **null hypothesis** H_0 and the **alternative hypothesis** H_1 .
- Step 2:* State the **significance level** α .
- Step 3:* Calculate the value of the **test statistic**: $\chi^2_{\text{calc}} = \sum \frac{(f_{\text{obs}} - f_{\text{exp}})^2}{f_{\text{exp}}}$.
- Step 4:* Use technology to calculate the **p-value**, using $\text{df} = \text{number of categories} - 1$.
- Step 5:* Reject H_0 if $p\text{-value} \leq \alpha$.
- Step 6:* Interpret your decision in the context of the problem. Write your conclusion in a sentence.

SUMMARY OF THE χ^2 TEST FOR INDEPENDENCE

- Step 1:* State the **null hypothesis** H_0 and the **alternative hypothesis** H_1 , which have the form:
 H_0 : the variables are independent
 H_1 : the variables are dependent.
- Step 2:* State the **significance level** α .
- Step 3:* Calculate **df** = $(r - 1)(c - 1)$ where r and c are the number of rows and columns of the contingency table respectively.
- Step 4:* Construct the **expected frequency table** and calculate the value of the **test statistic**:
 $\chi^2_{\text{calc}} = \sum \frac{(f_{\text{obs}} - f_{\text{exp}})^2}{f_{\text{exp}}}$.
- Step 5:* Use technology to calculate the **p-value**. *or* Find the critical value χ^2_{crit} for the test.
- Step 6:* Reject H_0 if $p\text{-value} \leq \alpha$ *or* if $\chi^2_{\text{calc}} \geq \chi^2_{\text{crit}}$.
- Step 7:* Interpret your decision in the context of the problem. Write your conclusion in a sentence.

- 4 f very strong, negative, non-linear correlation



ERRATA

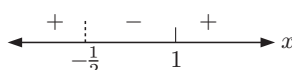
Mathematics: Applications and Interpretation SL

First edition - 2019 initial print

The following errata were made on 29/Apr/2020

page 63 SECTION 3E Example 9, last lines of solution should include sign diagram:

Since $(x - 1)$ and $(2x + 1)$ are single factors, the signs alternate.



The following errata were made on 02/Apr/2020

page 445 ANSWERS EXERCISE 3D Question 4 parts **c iv** and **d iv**, should read:

- 4 c**
- i y -intercept 2, no x -intercepts
 - ii min. turning point $(0, 2)$
 - iii no asymptotes
 - iv Domain is $\{x \mid x \in \mathbb{R}\}$, Range is $\{y \mid y \geq 2\}$
- d**
- i x -intercepts -2 and 2 , no y -intercept
 - ii no turning points
 - iii no asymptotes
 - iv Domain is $\{x \mid x \leq -2 \text{ or } x \geq 2\}$, Range is $\{y \mid y \geq 0\}$

The following errata were made on 30/Mar/2020

page 286 REVIEW SET 11B Question 3 **c**, should read:

- 3** The tangent to $y = x^3 + ax^2 - 4x + 3$ at $x = 1$ is parallel to the line $y = 3x$.
- a Find a .
 - b Find the equation of the tangent at $x = 1$.
 - c Where does the tangent **meet** the curve again?

page 352 CHAPTER 14 INVESTIGATION 1 Question 1, change for simplicity:

What to do:

- 1** Click on the icon to access the demonstration. It shows the graph of the binomial distribution for $X \sim B(n, p)$. Set $n = 25$ and $p = 0.1$.
- a What is the mode of X ?
 - b Describe the shape of the distribution.

page 389 EXERCISE 16B Question 1, should read:

- 1** A sample of size 36 is taken. The sample mean $\bar{x} = 23.75$ and the sample standard deviation $s = 3.97$. We are required to test the hypothesis $H_0: \mu = 25$ against $H_1: \mu < 25$.
- a Find:
 - i the test statistic
 - ii the p -value.
 - b What decision should be made at a 5% level?

page 442 **ANSWERS EXERCISE 1C** Questions **5**, **13**, and **15**, should read:

- 5** **a** 1.055 km **b** 9.715 km **c** 10.05 km
For distances < 10 km, the watch is accurate to ± 0.005 km.
For distances > 10 km, the watch is accurate to ± 0.05 km.

- 12** $1092.25 \pm 34 \text{ cm}^2$ **13** $31.875 \text{ cm}^2 < A < 40.375 \text{ cm}^2$
14 $196.5 \pm 52.125 \text{ cm}^3$ **15** $1502.11 \text{ cm}^2 < V < 1545.69 \text{ cm}^3$

page 442 **ANSWERS EXERCISE 1D** Question **11 b ii**, should read:

- 11** **a** ≈ 4.40 hours ($\approx 4 \text{ h } 24 \text{ min } 5 \text{ s}$)
 b **i** $\approx 45.7 \text{ s}$ **ii** $\approx 0.289\%$

page 443 **ANSWERS EXERCISE 3A** Question **7 a**, should read:

- 7** **a** $y^2 = x$ is a relation but not a function.
 $y = x^2$ is a function (and a relation).
 $y^2 = x$ has a horizontal axis of symmetry (the x -axis).
 $y = x^2$ has a vertical axis of symmetry (the y -axis).
 Both $y^2 = x$ and $y = x^2$ pass through $(0, 0)$ and $(1, 1)$.
 $y^2 = x$ is a rotation of $y = x^2$ clockwise through 90°
 about the origin or $y^2 = x$ is a reflection of $y = x^2$ in
 the line $y = x$.

page 491 **ANSWERS EXERCISE 14F** Question **c i**, should read:

- 1** **c** **i** $\mu = 4.8$, $\sigma \approx 0.980$

page 493 **ANSWERS EXERCISE 15B.1** Question **10 a**, should read:

- 10** **a** $\mu \approx 176 \text{ g}$, $\sigma \approx 24 \text{ g}$ **b** $\approx 81.85\%$

page 493 **ANSWERS EXERCISE 15B.2** Question **10 b**, should read:

- 10** **a** $\approx 84.1\%$ **b** ≈ 0.879

The following erratum was made on 22/Oct/2019

page 444 **ANSWERS EXERCISE 3C** Question **1 b**, should read:

- 1** **b** Domain is $\{x \mid x > 0\}$, Range is $\{y \mid y = 2, 3, 5, 7, \text{ or } 9\}$

The following errata were made on 02/Sep/2019

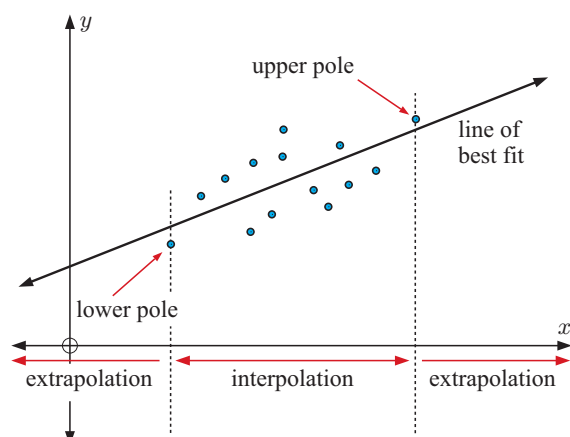
page 113 **SECTION 5C Interpolation and Extrapolation**, should read:

INTERPOLATION AND EXTRAPOLATION

Consider the data in the scatter diagram alongside. The data with the highest and lowest values are called the **poles**.

The **line of best fit** for the data is also drawn on the scatter diagram. We can use this line to predict the value of one variable for a given value of the other.

- If we predict a y value for an x value **in between** the poles, we say we are **interpolating** in between the poles.
- If we predict a y value for an x value **outside** the poles, we say we are **extrapolating** outside the poles.



page 114 **SECTION 5C Interpolation and Extrapolation**, first line should read:

For example, consider the **line of best fit** for the data in the **Opening Problem**. It can be used to predict the distance a discus will be thrown by an athlete of a particular age.

page 182 **REVIEW SET 7B Question 12 a**, should read:

- 12** Abbas wanted to test the sound intensity of the speakers in the local hall. He set the output to a constant power, and took measurements at different distances. The results are given below.

Distance (d m)	1	5	10	15	20
Sound intensity (I W m ⁻²)	63.7	2.55	0.637	0.283	0.159

- a** Abbas thinks that $I \propto \frac{1}{d}$. By calculating the value of $I \times d$ for each data point, show that he is incorrect.

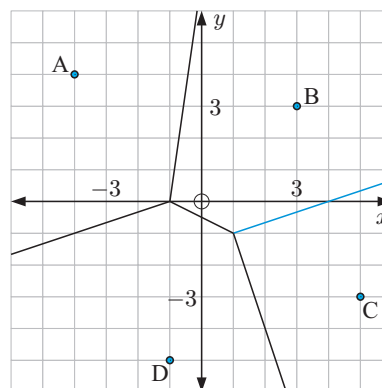
page 316 **EXERCISE 13B Question 5 b**, should integrate with respect to x :

- 5 b** For a positive function $f(x)$, $\int_2^5 f(x) \, dx = 10$, and $\int_5^9 f(x) \, dx = 12$. Find:

i $\int_5^5 f(x) \, dx$ **ii** $\int_2^9 f(x) \, dx$

page 438 **REVIEW SET 17A Question 6 c**, should read:

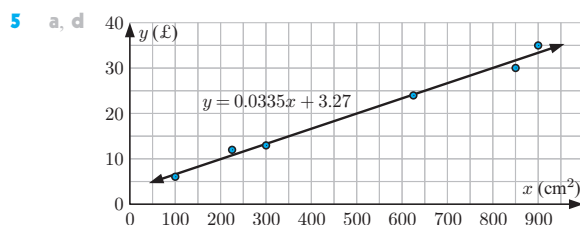
- 6** Consider the Voronoi diagram alongside.
- a** Find the equation of the blue edge.
 - b** Identify the site which is closest to:
 - i** $(2, -1)$ **ii** $(-5, -2)$
 - c** Redraw the Voronoi diagram with a new **site** added at $E(-3, -6)$.
 - d** Does the addition of site E affect your answers to **b**?



page 443 **ANSWERS REVIEW SET 1B Question 6 b**, should read:

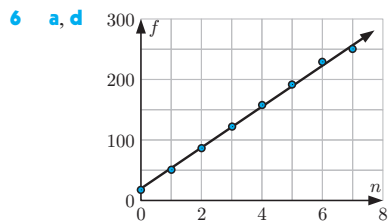
- 6 a** $14.85 \text{ s} < t < 14.95 \text{ s}$ **b** $6.66 \text{ ms}^{-1} < s < 6.77 \text{ ms}^{-1}$

page 458 **ANSWERS REVIEW SET 5B Question 5 c**, should read:



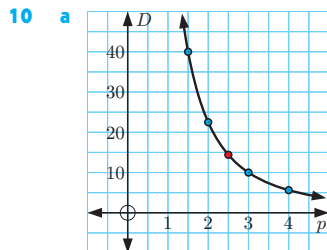
- b** $r \approx 0.994$ **c** There is a very strong, positive, **linear** correlation between *area* and *price*.
e $\approx £43.42$, this is an extrapolation, so it may be unreliable.

page 458 ANSWERS REVIEW SET 5B Question 6 a, should read:



There is a very strong, positive, **linear** correlation between number of waterings and flowers produced.

page 467 ANSWERS REVIEW SET 7A Question 10 a, should include point:



page 492 ANSWERS REVIEW SET 14B Questions 6 a and 9 a, should read:

- 6 a The probability of rolling a two is not the same for each die.
So X is not a binomial random variable.

b

x	0	1	2
$P(X = x)$	$\frac{15}{24}$	$\frac{1}{3}$	$\frac{1}{24}$

c $\frac{5}{12}$

7 $a = 0.15$, $b = 0.35$

8 a $E(X) = 2.1$ b $E(Y) = 1.9$

- 9 a The probability of spinning a 3 is the same for each spin.

page 499 ANSWERS EXERCISE 17B Question 11 a, should read:

- 11 a There is a cell which does not contain a site.